

ENERGETIC NEUTRAL ATOMS AROUND HD 209458b: ESTIMATIONS OF MAGNETOSPHERIC PROPERTIES

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ABSTRACT

HD 209458b is an exoplanet found to transit the disk of its parent star. Observations have shown a broad absorption signature about the Ly α stellar line during transit, suggesting the presence of a thick cloud of atomic hydrogen around the “hot Jupiter” HD 209458b. This work expands on an earlier work studying the production of energetic neutral atoms (ENAs) as a result of the interaction between the stellar wind and the exosphere. We present an improved flow model of HD 209458b and use stellar wind values similar to those in our solar system. We find that the ENA production is high enough to explain the observations, and we show that—using expected values for the stellar wind and exosphere—the spatial and velocity distributions of ENAs would give absorption in good agreement with the observations. We also study how the production of ENAs depends on the exospheric parameters and establish an upper limit for the obstacle standoff distance at approximately 4–10 planetary radii. Finally, we compare the results obtained for the obstacle standoff distance with existing exomagnetospheric models and show how the magnetic moment of HD 209458b can be estimated from ENA observations.

Key words: methods: data analysis – methods: numerical – stars: winds, outflows

Online-only material: color figures

1. INTRODUCTION

HD 209458b is a Jupiter-type planet for which several transits in front of its parent star were discovered in 2000 (Charbonneau et al. 2000; Henry et al. 2000). Observations with the *Hubble Space Telescope* (*HST*) show absorption in the Ly α line (at 1215.67 Å) during transit, revealing the occurrence of a thick cloud of atomic hydrogen around HD 209458b (Vidal-Madjar et al. 2003; Ben-Jaffel 2007). The estimation of the absorption rate has been done independently by Vidal-Madjar et al. (2003) and Ben-Jaffel (2007). Vidal-Madjar et al. (2003) find a higher absorption rate and interprets the absorption as hydrogen atoms in the exosphere undergoing hydrodynamic escape, further accelerated by the stellar radiation pressure (Vidal-Madjar et al. 2003, 2004, 2008). Ben-Jaffel (2007) finds a lower absorption rate and concludes that there are no signs of hydrodynamic escape (Ben-Jaffel 2007, 2008). Based on the interpretation of *HST* data done by Vidal-Madjar et al. (2003), an alternative explanation was suggested by Holmström et al. (2008a), hereafter H08, showing that energetic neutral atoms (ENAs) created by charge exchange between the stellar wind and the exosphere can solely explain the cloud of high-velocity hydrogen. The reported absorption of the Ly α line is characterized by a significant broadening and, according to Vidal-Madjar et al. (2003, 2004), by a slight shift toward the shorter wavelengths. These two observed features can be reproduced by the ENA model presented in H08, while they cannot be reproduced without ENAs in that model. However, it should be noted that Ben-Jaffel (2007) interprets the shift toward shorter wavelengths as mostly due to thermal broadening. ENAs resulting from the interaction of the solar wind with a planetary environment have been observed at Earth (Collier et al. 2001), Mars (Futaana et al. 2006), and Venus (Galli et al. 2008), and charge exchange with stellar wind protons around

HD 209458b can explain the high-velocity hydrogen in analogy with these observations in our solar system. Here we study how an improved flow model for the stellar wind will affect the ENA production. The resulting flow will be a gas dynamic flow around the obstacle (Spreiter & Stahara 1980). In particular, the changes to the flow model with respect to Holmström et al. (2008a) are as follows.

1. Stellar wind protons reaching the obstacle boundary are now reflected at the obstacle boundary to model the deflected stellar wind flow around the obstacle. In the earlier model, the protons arriving at the obstacle boundary were deleted.
2. The forces on hydrogen atoms in H08 were inaccurate at large distances from the planet since only the Coriolis force from the rotating coordinate system represented the gravity of the star. Star gravity and centrifugal force on the particles are now included.

We also investigate if it is possible to infer properties of the planetary obstacle to the stellar wind from the ENA observation, e.g., if the planet is magnetized or not.

2. PLASMA FLOW MODEL

In what follows, the coordinate system used is centered at the planet and has its x -axis toward the star, the y -axis opposite the planet's orbital velocity v_p , and the z -axis completes the right-handed coordinate system. The default values of physical constants and parameters used in the simulation are listed in Table 1. Default values of numerical parameters can be found in Table 2. The outer boundary of the simulation domain is the box $x_{\min} \leq x \leq x_{\max}$, $y_{\min} \leq y \leq y_{\max}$, and $z_{\min} \leq z \leq z_{\max}$. The inner boundary is a sphere of radius R_0 .

The conic obstacle to the stellar wind protons is defined by the surface (X, ρ) , such that $X = -\rho^2/(20R_p) + X_0$, where R_p is

Table 1

Default Values of Physical Parameters, and Values of Constants Used in the Simulations, Unless Otherwise Noted

Parameter	Symbol	Value	
Star radius	...	7.0×10^8 m	$= 1.1 R_{\text{Sun}}$
Planet radius	R_p	9.4×10^7 m	$= 1.3 R_{\text{Jup}}$
Planet mass	...	1.3×10^{27} kg	$= 0.7 M_{\text{Jup}}$
Orbital distance	...	6.7×10^9 m	$= 0.045$ AU
Orbital velocity	v_p	1.4×10^5 m s ⁻¹	...
Angular velocity	ω	2×10^{-5} rad s ⁻¹	...
Inner boundary radius*	R_0	2.7×10^8 m	$= 2.8 R_p$
Inner boundary temperature*	...	0.6×10^4 K	...
Inner boundary density*	n	4×10^{13} m ⁻³	...
H–H cross section	...	10^{-21} m ²	...
H–H ⁺ cross section ^a	...	$\approx 2 \times 10^{-19}$ m ²	...
UV absorption rate	τ_r	0.35 s ⁻¹	...
Photoionization rate	τ_i	7×10^{-5} s ⁻¹	...
Obstacle standoff distance	X_0	4×10^8 m	$= 4.3 R_p$
Stellar wind density*	...	3.5×10^9 m ⁻³	...
Stellar wind velocity*	v_{sw}	4.5×10^5 m s ⁻¹	...
Stellar wind temperature	T_{sw}	1×10^6 K	...

Notes. A star (*) indicates a value different from H08.

^a Energy dependent from Lindsay & Stebbings (2005).

Table 2

Default Numerical Parameter Values Used in the Simulations

Parameter	Symbol	Value
...	x_{min}	-5.0×10^9 m $= -53 R_p$
...	x_{max}	2.0×10^9 m $= 21 R_p$
...	y_{min}	-7.0×10^9 m $= -74 R_p$
...	y_{max}	7×10^9 m
...	z_{min}	-3.5×10^9 m $= -37 R_p$
...	z_{max}	3.5×10^9 m
Number of particles per meta-particle*	N_m^a	3.44×10^{32}
Number of cells	...	16×10^6
Final time	t_{max}	10^5 s
Time step	Δt	25 s

Notes. A star (*) indicates a value different from H08.

^a We tried to keep the total number of meta-particles relatively independent of exospheric density. N_m therefore changed with approximately $1/\Delta_\rho$ for the different exospheric scenarios (see Section 3.1), where Δ_ρ is the change in the exospheric density.

the planet's radius and X_0 is the obstacle standoff distance. Here ρ is the distance to the planet–star line, aberrated by an angle of $\arctan(v_p/v_{\text{sw}})$ to account for the finite stellar wind speed v_{sw} relative to the planet's orbital speed v_p . The location of the obstacle boundary, the stellar wind direction, and the orbital velocity direction are shown in Figure 1.

2.1. Simulation Description

At the start of the simulation the domain is devoid of particles. Then hydrogen meta-particles are launched from the inner boundary at a rate of 300 meta-particles per second. Each meta-particle corresponds to N_m hydrogen atoms. The location on the inner boundary of each launched particle is randomly drawn. The velocity of each launched particle is randomly drawn from a probability distribution proportional to

$$(\mathbf{n} \cdot \mathbf{v}) e^{-a|\mathbf{v}|^2},$$

where \mathbf{n} is the local unit surface normal, \mathbf{v} is the velocity of the particle, and $a = m/(2k_B T)$, m is the mass of a neutral,

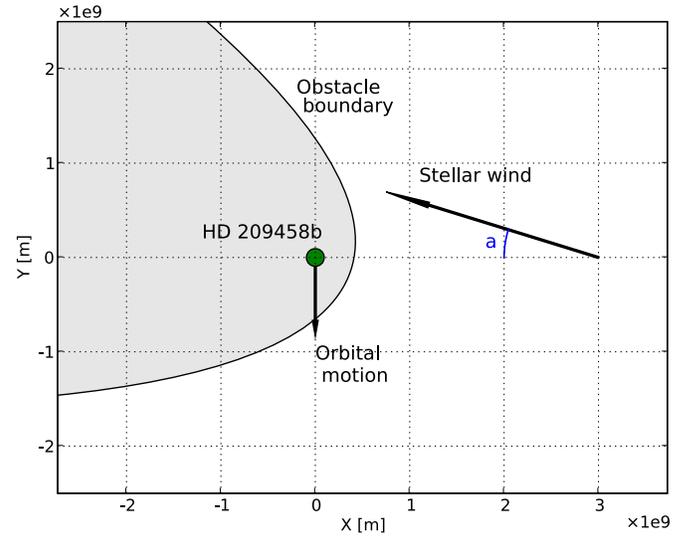


Figure 1. Illustration of near-planet geometry and the ENA production region. This work only considers ENAs produced outside of the obstacle boundary—a magnetopause in case HD 209458b has an intrinsic magnetic field or an induced magnetospheric boundary otherwise—which is the unshaded area. The plot shows the shape of the obstacle boundary for the default parameters as in Table 1. The used aberration angle $a = \arctan(v_p/v_{\text{sw}})$, explained in Section 2, is also shown.

(A color version of this figure is available in the online journal.)

k_B is Boltzmann's constant, and T is the temperature (at the exobase position). The distribution used is not Maxwellian, but the distribution of the flux through a surface (the exobase), given a Maxwellian distribution at the location (Garcia 2000). The number of flux through the surface is $n/\sqrt{4\pi a}$, where n is the inner boundary hydrogen density, for a total production rate of $nR_0^2\sqrt{8\pi k_B T/m}$. After an hydrogen atom is launched from the inner boundary, we numerically integrate its trajectory with a time step of 25 s.

Before each time step we also fill the x -axis shadow cells (cells just outside the simulation domain) with proton meta-particles of the same weight as for hydrogen, N_m . After each time step the shadow cells are emptied of protons. The protons are drawn from a Maxwellian distribution with temperature T_{sw} and bulk velocity v_{rel} . The relative velocity at the planet, v_{rel} , is related to the stellar wind velocity and the planet's orbital velocity by $v_{\text{rel}}^2 = v_{\text{sw}}^2 + v_p^2$. At the obstacle the stellar wind is reflected in the surface normal. The boundary conditions in the y - and z -directions are periodic.

Between time steps, the following events can occur for an exospheric atom:

1. Scattering of an UV photon. Following Hodges (1994) this occurs as an absorption of the photon (Δv of the hydrogen atom is opposite the star direction) followed by isotropic re-radiation (Δv of the hydrogen atom in a random direction). From Hodges (1994) we use a velocity change $\Delta v = 3.27$ m s⁻¹. The UV scattering rate is given in Table 1. The scattering rate is zero if the particle is in the shadow behind the planet.
2. Photoionization by a stellar photon occurs at a rate of τ_i when an exospheric hydrogen atom is outside the optical shadow behind the planet, and then the meta-particle is removed from the simulation.
3. Charge exchange with a stellar wind proton. If the hydrogen atom is outside the obstacle it can charge exchange with a stellar wind proton, producing an ENA. This is done

using the direct simulation Monte Carlo (DSMC) method described in the next section.

4. Elastic collision with another hydrogen atom, according to the DSMC method described in the next section.

All rates above are from Hodges (1994) for Earth, and average solar conditions, scaled by $(1/0.045)^2$ to account for the larger photon fluxes at the orbital distance of HD 209458b.

The forces acting on a hydrogen atom are the gravity of the planet \mathbf{G}_{pl} and of the star \mathbf{G}_{st} . Because of the rotation, at an angular rate of ω , the fictitious Coriolis, \mathbf{F}_{cor} , and centrifugal, \mathbf{F}_{cent} , forces also affect the hydrogen atoms. The total force, \mathbf{F}_{tot} , on a hydrogen atom is thus

$$\mathbf{F}_{\text{tot}} = \mathbf{G}_{\text{pl}} + \mathbf{G}_{\text{st}} + \mathbf{F}_{\text{cor}} + \mathbf{F}_{\text{cent}}. \quad (1)$$

2.2. Derivation of Stellar Parameters

The stellar wind density and temperature have also been scaled from average solar conditions for our Sun using relations given by Russell et al. (1988, p. 514). Given the close proximity of HD 209458b to its host star the choice of stellar wind parameters has to be looked at in some detail. At the Sun we distinguish between slow and fast solar wind, with the former being below about 400 km s^{-1} and the latter larger than 400 km s^{-1} , often even up to 800 km s^{-1} . Although there is temporal fluctuation on all timescales (Wurz 2005), it is for the purpose of this study sufficient to consider average values. Using a proton density of 7 cm^{-3} at Earth orbit translates to about 3500 cm^{-3} at the orbit of HD 209458b using a quadratic scaling. With the radius of HD 209458 being 1.1 times the solar radius, the location of the planet is at $9.6R_{\text{st}}$, with R_{st} being the stellar radius. At the Sun, this distance is close to the acceleration region of the solar wind. For the Sun, several measurements show that the acceleration of the solar wind occurs close to the Sun. For the fast solar wind, Grall et al. (1996) showed that it is fully developed within $10R_{\text{st}}$. These and other measurements have been summarized and compared to theoretical models by Esser et al. (1998). Based on this work we would expect a stellar wind speed at HD 209458b of about 800 km s^{-1} . For the slow solar wind there are also measurements of its acceleration. Kohl et al. (1998) show that protons have already 300 km s^{-1} at $4R_{\text{st}}$, and Sheeley et al. (1997) found similar results with little acceleration beyond $7R_{\text{st}}$. Assuming HD 209458b is in the slow solar wind regime the stellar wind velocity would be 300 km s^{-1} . Since we do not know what stellar wind regime HD 209458b is actually experiencing, a stellar wind speed of 450 km s^{-1} is chosen. Note that for our Sun, the slow solar wind regime is more likely to occur in the ecliptic plane (McComas et al. 2003). We can also scale the magnetic field to regions close to the star, which gives a stellar wind magnetic field of $3.5 \mu\text{T}$ using a solar wind magnetic field of 10 nT at 1 AU . That magnetic field, together with the proton density, gives an Alfvén speed $v_A = 1540 \text{ km s}^{-1}$, which suggests that the stellar wind at HD 209458b is sub-Alfvénic and a bow shock will not develop (Erkaev et al. 2005).

The photon–hydrogen collision rate, τ_r as shown in Table 1, is chosen lower than a scaled value of $0.6\text{--}1.6 \text{ s}^{-1}$ averaged over a solar cycle. This was done to approximate the actual velocity-dependent radiation pressure which decreases with velocity for the hydrogen atoms as they move out of the central Ly α peak in the velocity spectrum. For the radiation pressure and photoionization event rates, τ , after each time step, for each meta-particle, we draw a random time from an exponential distribution with mean τ , and the event occur if this time is

smaller than the time step. Note that we only consider ENAs produced outside the obstacle, so the fluxes presented here are a lower bound. Additional ENAs are produced inside, but including those would require a complete ion flow model.

2.3. Collisions

The collisions between hydrogen atoms are modeled using the DSMC method (Bird 1976), where we divide the computational domain into cells. Then after each time step the particles that are in the same cells are considered for hard sphere collisions. From Equation (1.6) in Bird (1976), the frequency of collisions experienced by a single particle is $\nu = n\bar{\sigma}v_r$, where n is the total number density of all species, σ is the total collisional cross section, and v_r is the relative velocity between the particle and the particles in the surrounding gas. The bar denotes average. From this we get that the total collision frequency in a volume is

$$\frac{1}{2}n\nu = \frac{1}{2}n^2\bar{\sigma}v_r. \quad (2)$$

For each pair of particles, their collision probability is proportional to σv_r . For a cell, we estimate n by $N_c N_m / V_c$, where N_c is the number of meta-particles in the cell, N_m is the number of particles per meta-particle, and V_c is the cell volume.

To avoid an operation count proportional to N_c^2 , following Garcia (2000, p. 359), we do not directly compute the averages. Instead we estimate a maximum value of σv_r , $(\sigma v_r)_{\text{max}}$, and use that in Equation (2) to compute the number of trials. For each trial we then draw a random pair and a random number R on $[0, (\sigma v_r)_{\text{max}}]$. If $\sigma v_r > R$ for the chosen pair, the collision is accepted.

The random pair above is uniformly distributed if N_m is the same for all particles, as is the case for these simulations.

2.4. Time Integration

To avoid energy dissipation, the time advance of the particles from time t to time $t + \Delta t$ is done using the symplectic integrators derived by Candy & Rozmus (1991),

$$\mathbf{x} \leftarrow \mathbf{x} + c_k \Delta t \mathbf{v}, \quad (3)$$

$$\mathbf{a} \leftarrow \mathbf{a}(\mathbf{x}, t), \quad (4)$$

$$\mathbf{v} \leftarrow \mathbf{v} + d_k \Delta t \mathbf{a}, \quad (5)$$

$$t \leftarrow t + c_k \Delta t, \quad (6)$$

for $k = 1, \dots, n$. Here \mathbf{x} are the particle positions, \mathbf{v} are the velocities, and $\mathbf{a}(\mathbf{x}, t)$ are the accelerations. The coefficients c_k and d_k can be found in Candy & Rozmus (1991). The global order of accuracy is n , and $n = 2$ corresponds to the Leapfrog method. In this work we have used $n = 4$.

2.5. Software

We use an existing software, FLASH, developed at the University of Chicago (Fryxell et al. 2000), which provides adaptive grids and is fully parallelized, and which we have extended to do DSMC modeling of planetary exospheres (Holmström 2006). FLASH is a general parallel solver for compressible flow problems. It is written in Fortran 90, well structured into modules, and open source. The parallelization is to a large extent handled by the PARAMESH (MacNeice et al. 2000) library which implements a block-structured adaptive Cartesian grid with the Message–Passing Interface (MPI) library as the underlying communication layer.

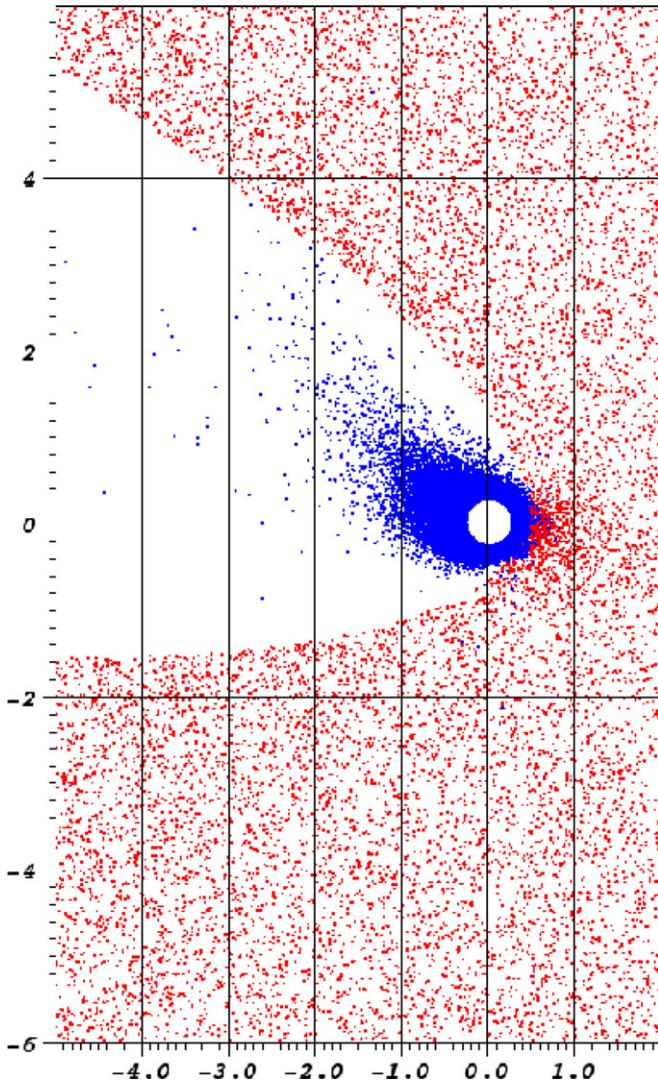


Figure 2. Flow of stellar wind protons and the exospheric hydrogen cloud seen from above in the direction of the negative z -axis (perpendicular to the orbital plane). Each point corresponds to a neutral hydrogen (red or dark), or a proton (blue or lighter) meta-particle in the slice $-10^7 \text{ m} \leq z \leq 10^7 \text{ m}$. The scale on the axes is 10^9 m . The circle without particles corresponds to the inner boundary of the simulation, and the large area without protons corresponds to the assumed obstacle to the stellar wind, on which the protons are reflected.

(A color version of this figure is available in the online journal.)

2.6. Ly α Attenuation

Given the positions of all the hydrogen meta-particles at a certain time, we now proceed to compute how they attenuate the stellar Ly α radiation. We discretize the yz -plane using a grid. For each cell in the grid we compute the velocity spectrum of all hydrogen atoms in the column along the x -axis corresponding to the cell. This velocity spectrum can be converted into a frequency spectrum using the relation $f = f_0 + v/\lambda_0$, where v is the velocity, $\lambda_0 = 1215.67 \times 10^{-8} \text{ cm}$, and $f_0 = c/\lambda_0$. This spectrum, $h(f)$, is normalized to have unit integral. Assuming only single scattering, the attenuation factor $A(f)$ at each frequency is then given as

$$A(f) = 1 - e^{-ngfah(f)}, \quad (7)$$

where n is the column density, the weighted oscillator strength $gf = 2 \times 0.4162$ (Ralchenko et al. 2008), and $a = \pi e^2/(m_e c) = 0.026 \text{ Hz cm}^2$. This attenuation factor is then

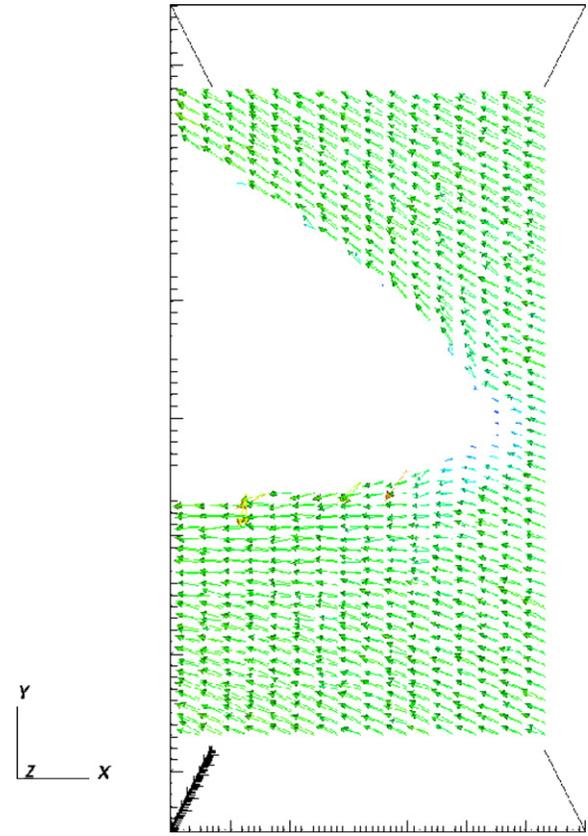


Figure 3. Velocity vectors of stellar wind protons in the orbital plane. The velocity shown is the average for all particles in a cell.

(A color version of this figure is available in the online journal.)

averaged over all columns in the yz -grid, except for those whose center falls outside the projected limb of the star. Columns over the planet disk are assigned an attenuation of 1. The projected limb of the star is shifted downward (smaller z) by $4.58 \times 10^8 \text{ m}$ to account for the planet orbit's inclination. This attenuation is then applied to the observed spectrum. At each velocity we simply multiply the observed spectrum by the attenuation factor. If we also include the effects of natural broadening and Doppler broadening by the atmosphere inside our inner boundary sphere of radius R_0 , the result is that an atmospheric column density of at least 10^{20} cm^{-2} is needed for any effect to be visible in the model spectra. This is much larger than the density in published atmospheric models.

3. MODEL RESULTS

We describe here the obtained plasma flow and how well the obtained ENA production fits the *HST* observations. Using a higher stellar wind velocity than in H08 we get an obstacle shape pointing more radially toward the star. The hydrogen cloud is still cometary shaped but with a smaller bend compared to results in H08. A slice of the simulations is shown in Figure 2, displaying stellar wind protons and the hydrogen atoms. Visibly we can see that the hydrogen cloud reaches (with significant density) outside the obstacle boundary and can produce ENAs by charge exchange with stellar wind protons. In Figure 3, we also show vectors for the proton flow to illustrate how they are now deflected around the obstacle.

The computed attenuation at mid-transit is shown in Figure 4. The ENA production produces a visible asymmetry in the $[-200, 200] \text{ km s}^{-1}$ interval and is high enough to explain

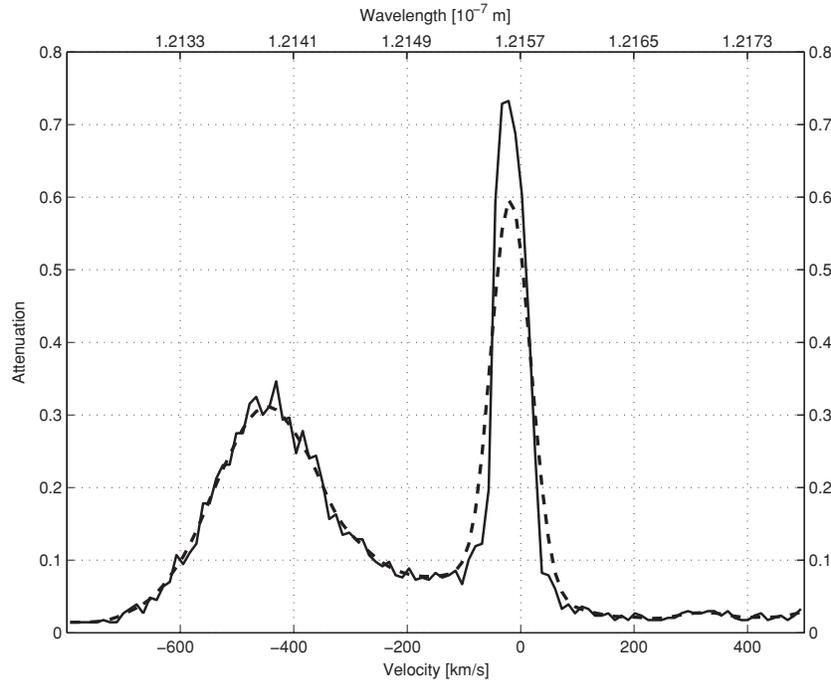


Figure 4. Bold line shows the attenuation at mid-transit as a function of hydrogen x -axis velocity, computed with Equation (7). Negative velocities are toward the observer. The dashed curve is a convolution of the bold line with a Gaussian of width 20 km s^{-1} to illustrate the effect of the resolution of the observation.

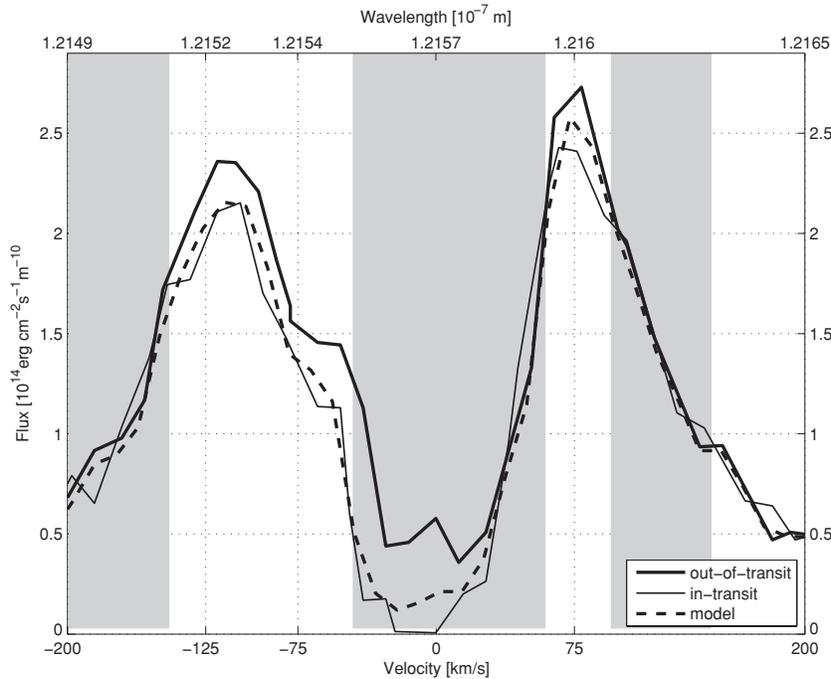


Figure 5. Obtained attenuation spectrum and comparison with observations. The bold line is the observed profile before transit and the thinner line below it is the observed profile during transit. The dashed line is the modeled profile, constructed by applying the attenuations computed from the simulations to the observed profile before transit. The modeled profile is computed at the instant of mid-transit.

the observed Ly α attenuation. Figure 5 shows the resulting attenuation spectra from our model with the default parameter settings along with observational data as reported by Vidal-Madjar et al. (2003). The analysis is focused on the wavelength intervals for which atomic hydrogen absorption has been observed, and where there is no geocoronal observations (Vidal-Madjar et al. 2003). We find that the fit to observations is as good as in H08.

Introducing star gravity and centrifugal force makes particles at smaller radial distances from the star more affected by the

gravity of the star than the centrifugal force. The result is that the exosphere between the star and the planet is shifted toward the star, thus increasing the number of exospheric particles outside the obstacle boundary. This increases the number of produced ENAs, shown in Figure 6, but the number of ENAs in the velocity region -130 to 100 km s^{-1} is virtually unchanged.

We can also investigate the time dependence of the attenuation. The attenuation as a function of orbital phase is shown in Figure 7. We see that the comet-like hydrogen cloud gives rise

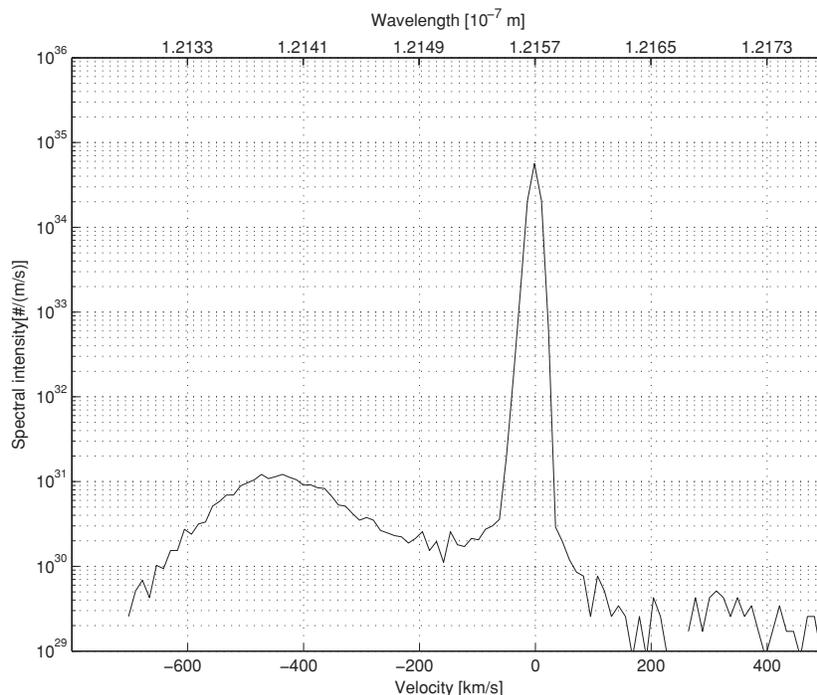


Figure 6. Velocities of the hydrogen atoms. The modeled x -axis (planet–star) velocity spectrum of hydrogen atoms in front of the star at the moment of mid-transit, not including atoms in front of or behind the planet disk. The low-velocity hydrogen, seen as a peak in the spectrum between -75 and 25 km s^{-1} , are mostly exospheric but the rest of the spectrum displays large number of ENAs produced by charge exchange with the stellar wind.

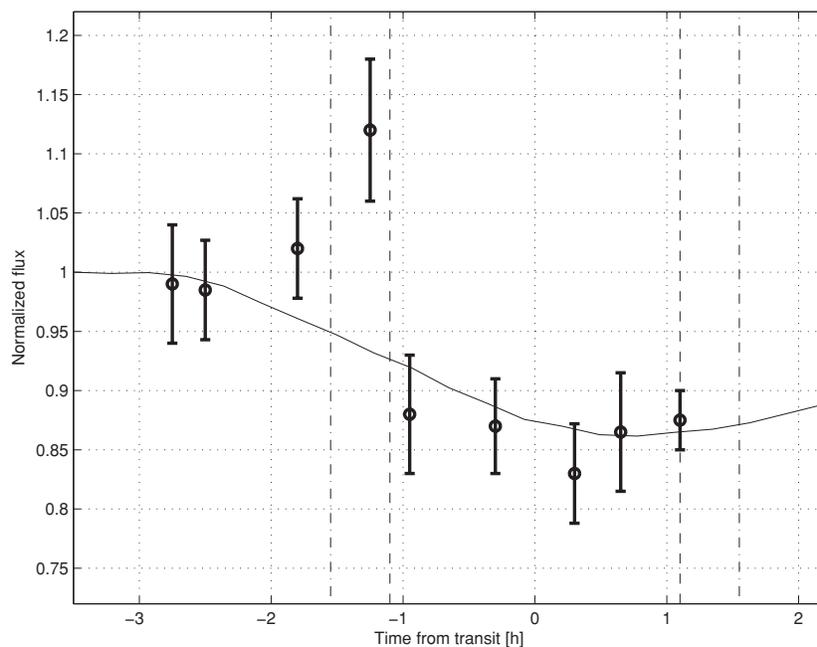


Figure 7. Relative flux of $\text{Ly}\alpha$ as a function of HD 209458’s system phase. Time is centered around mid-transit. The curve is the attenuation as obtained by our model, and circles with error bars are observational data as reported by Vidal-Madjar et al. (2003). The dashed lines mark the first and second contacts at the beginning and end of the transit.

to an asymmetry in attenuation over time, making attenuation post-transit higher than pre-transit for an equal time shift. The curve of attenuation over time is in agreement with the observations by Vidal-Madjar et al. (2003) and is also similar to their modeled attenuation curve.

3.1. Sensitivity to Exospheric Parameters

Since the density and temperature profiles of the exosphere are uncertain we explore a range of values for both these parameters. At our inner boundary the temperature, based

on the model by Penz et al. (2008), is approximately half of the temperature estimated by, for example, Yelle (2004). For the exospheric density our number is approximately 10 times less than the number estimated by García Muñoz (2007). To study the ENA production as a function of various exospheric conditions we chose nine different scenarios by testing with higher and lower values for both density and temperature. Exospheric density was varied up and down by a factor of 10 at the inner boundary, where the original density is denoted by ρ_0 , giving $\rho_- = \rho_0/10$ and $\rho_+ = 10\rho_0$. Exospheric temperature

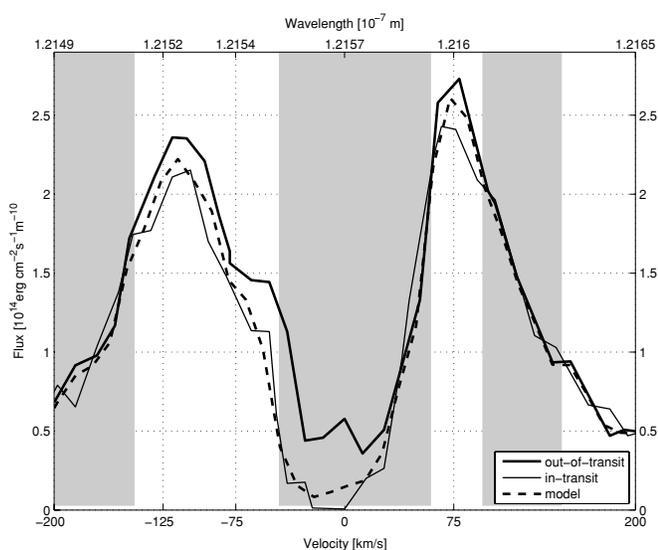


Figure 8. Effects on the attenuation and velocity spectra when increasing the exospheric density by a factor of 10.

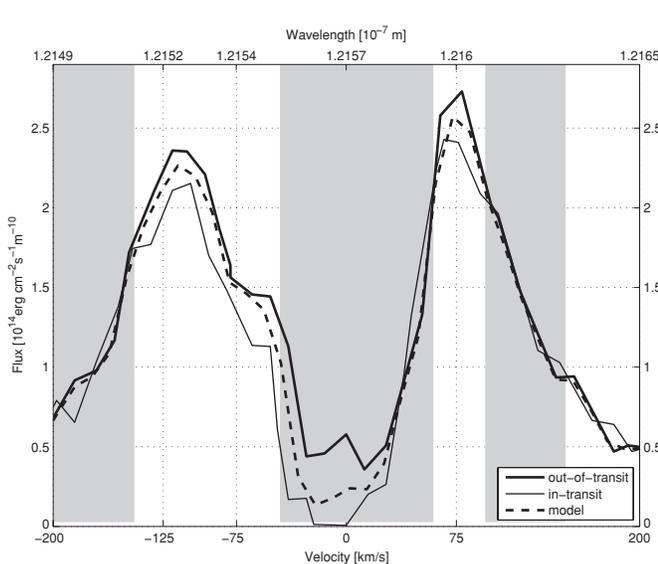


Figure 9. Effects on the attenuation and velocity spectra when decreasing the exospheric density by a factor of 10.

was varied up and down by a factor of 2 at the inner boundary, and analogously denoted by T_0 , $T_- = T_0/2$ and $T_+ = 2T_0$. For each exospheric scenario, the only remaining free parameter is the obstacle standoff distance.

Since we here only include ENAs produced outside of the obstacle boundary, exospheric temperature—determining the rate of decrease in density from the exobase—is apparently a more important factor for the ENA production than the exospheric density. Our model is less sensitive to the exospheric density parameter since this parameter can be said to determine only the peak density (at the exobase). The higher sensitivity to exospheric temperature than density can be seen by comparing the attenuation spectra in Figures 8–11. An increase in exospheric density does not effect the attenuation much, even though a decrease in density will reduce the attenuation significantly. In the velocity spectrum a probable cause for this asymmetry: a decreased exospheric density has reduced the number of hydrogen in the studied velocity intervals relatively more than other hydrogen. Using an exospheric temperature with twice the

default value we obtain an unreasonably high attenuation, while a decrease in temperature reduces the attenuation considerably.

4. OBSTACLE STANDOFF DISTANCE

Since ENA production depends on the planetary obstacle to the stellar wind, ENA observations can yield information on the obstacle. The size of the magnetosphere of an extrasolar planet cannot be measured directly, but it has implications on many processes. It determines the intensity of planetary radio emission (Desch & Kaiser 1984; Zarka et al. 1997; Farrell et al. 1999; Grießmeier et al. 2007), the protection of the planetary atmosphere against atmospheric loss by the solar wind and by CMEs (Grießmeier et al. 2004; Khodachenko et al. 2007a, 2007b; Lammer et al. 2007), and the protection of a planet against cosmic rays (Grießmeier et al. 2005b, 2009) which in turn can affect biomarker concentrations in the planetary atmosphere (Grenfell et al. 2007). To improve our understanding of these processes, good estimations for a magnetospheric

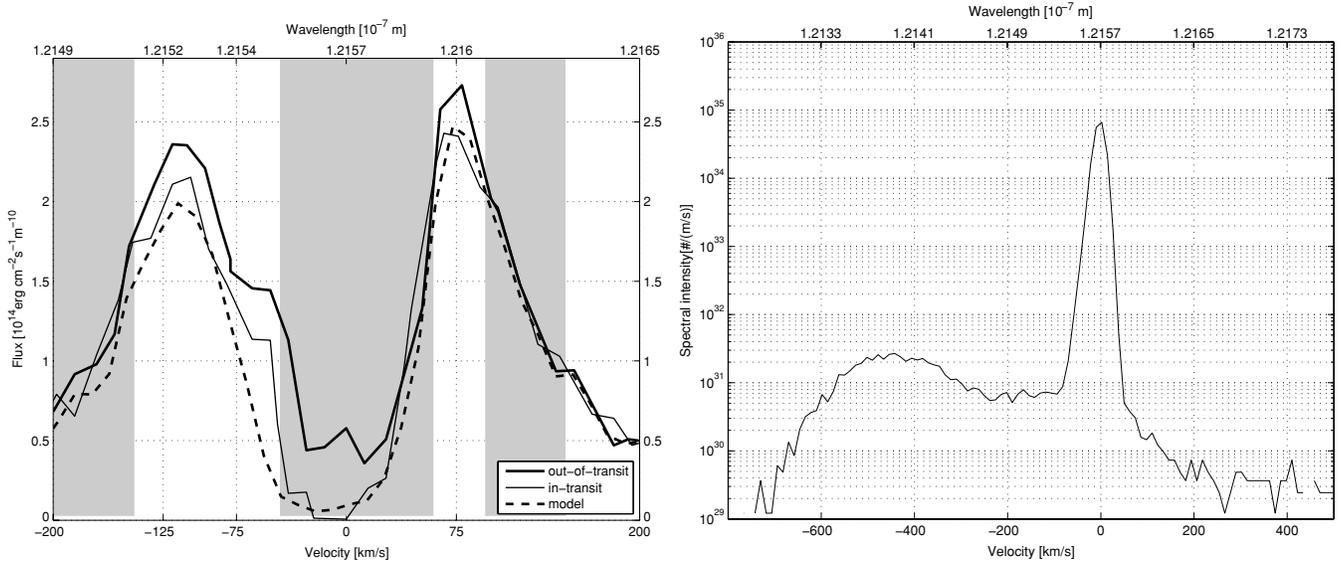


Figure 10. Effects on the attenuation and velocity spectra when increasing the exospheric temperature by a factor of 2.

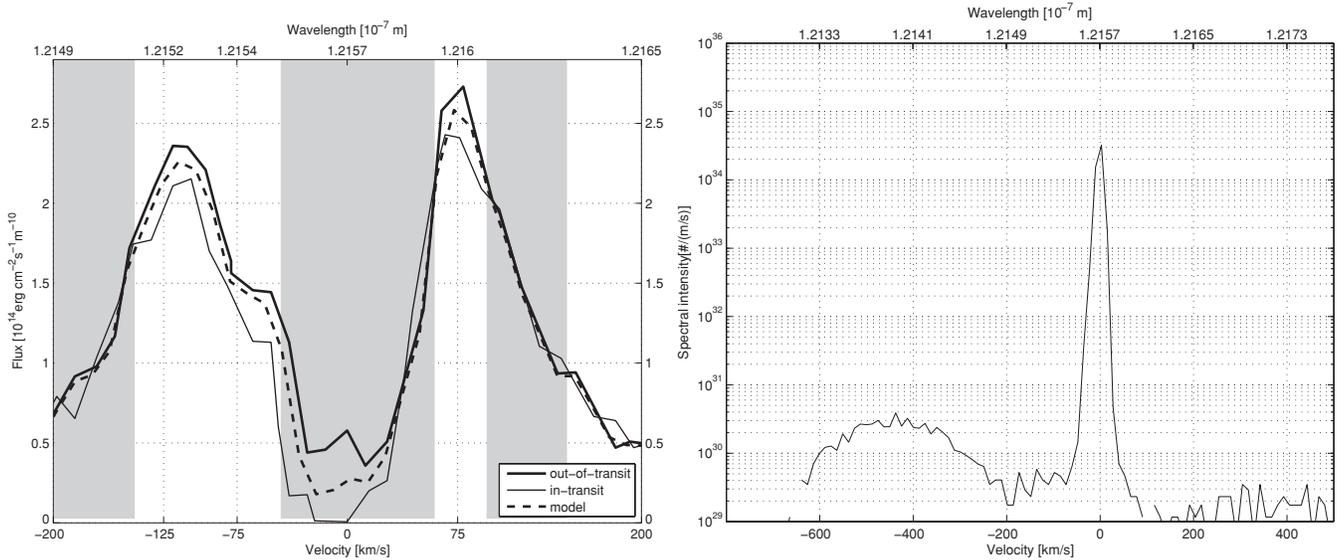


Figure 11. Effects on the attenuation and velocity spectra when decreasing the exospheric temperature by a factor of 2.

obstacle would be very helpful. Although model values exist for the size of exomagnetospheres, these models rely on the assumption that the planetary magnetic moment can be modeled in a simple way, which is sometimes disputed. In principle, ENA observations have the potential to discriminate between plausible and less plausible models. To demonstrate this, we here try to derive an approximate size of the magnetosphere and compare the results with those found by magnetospheric modeling.

4.1. Upper Limit on Obstacle Standoff Distance

By using the different exospheric parameters, described in Section 3.1, it is possible to determine an upper limit of the obstacle standoff distance for each set of parameters. We do this by increasing the obstacle standoff distance until it is impossible to get any attenuation with a reasonable stellar wind density. We chose $10,000 \text{ cm}^{-3}$ as a maximum reasonable stellar wind density and study the attenuation as we increase the obstacle standoff distance by steps of $2.1R_p$. The obtained upper limits

Table 3
Obtained Upper Bounds and Best Fit to Observations for Obstacle Standoff Distance as a Function of Exosphere Density and Temperature

Name	$\rho-T_-$	$\rho-T_0$	$\rho-T_+$	ρ_0T_-	ρ_0T_0	ρ_0T_+	ρ_+T_-	ρ_+T_0	ρ_+T_+
Upper limit	4.3	6.4	8.5	6.4	6.4	11	6.4	6.4	8.5
Best fit	$\leq 3.2^a$	$\leq 3.2^a$	$\leq 3.2^a$	$\leq 3.2^a$	4.3	6.4	$\leq 3.2^a$	4.3	6.4

Notes. The lengths are given in units of planetary radius R_p .
^a An entry of ≤ 3.2 means that a better fit could probably be found by decreasing the obstacle standoff below $3.2R_p$. Such simulations would not be accurate with the current model since we have used an inner boundary of $2.8R_p$.

as a function of exospheric parameters are shown in Table 3. For our default scenario we establish an upper limit of the obstacle standoff distance at $6.4R_p$.

4.2. Estimated Obstacle Standoff Distance

By varying the obstacle standoff distance we should be able to find a best fit for each exospheric scenario. We find that for

most scenarios the deviation compared to observations are still decreasing when we decrease obstacle distance down to $3.2R_p$. Due to computational limitations it is beyond the scope of this work to do simulations with an inner boundary below $2.8R_p$. We can therefore not find the value with best fit for most scenarios but can state that the value is $\leq 3.2R_p$. The best fit to observations for each exospheric scenario is shown in Table 3. For our default scenario we determine a best fit to observations at $4.4R_p$.

4.3. Comparison of Obstacle Distances to Magnetospheric Modeling

The magnetosphere is shaped by the interplay between the stellar wind flow and the planetary magnetic field. The size of the magnetosphere depends on the magnetic pressure (planetary magnetic field plus the field generated by the magnetopause currents) inside the magnetosphere and the stellar wind ram pressure outside the magnetosphere (Voigt 1995; Grießmeier et al. 2007). The contribution of other factors in the pressure balance (e.g., the thermal pressure) is negligible in the present case. In term of units normalized to Jupiter's units, the magnetospheric standoff distance R_M can then be written as

$$R_M \approx 40 R_{\text{Jup}} \left[\frac{\tilde{M}^2}{\tilde{n} \tilde{v}_{\text{rel}}^2} \right]^{1/6}. \quad (8)$$

Here, \tilde{M} is the planetary magnetic dipole moment in units Jupiter's magnetic moment (which is taken as $M_{\text{Jup}} = 1.56 \times 10^{27} \text{ Am}^2$; Cain et al. 1995). Similarly, the stellar wind velocity and density are taken relative to the values encountered at Jupiter's orbit: $\tilde{n} = n/n_{\text{Jup}}$ and $\tilde{v}_{\text{rel}} = v_{\text{rel}}/v_{\text{rel,Jup}}$, with $n_{\text{Jup}} = 2.0 \times 10^5 \text{ m}^{-3}$, and $v_{\text{rel,Jup}} = 520 \text{ km s}^{-1}$. The index "rel" for the stellar wind velocity is a reminder that we use the relative stellar wind velocity as seen from the planet (i.e., including the aberration effect by the planetary orbital velocity, cf. Section 2).

Taking the stellar wind parameters from Table 1, the magnetic moment is the only remaining free parameter required to obtain R_M . Conversely, the values obtained for R_M in the previous section (Table 3) allow us to test and constrain existing models on planetary magnetic moments. This is especially important as two different ideas exist: according to the first, the strength of the planetary magnetic dipole moment can be estimated from the planetary characteristics using simple scaling relations. This approach was taken in, e.g., Farrell et al. (1999), Lazio et al. (2004), Grießmeier et al. (2004, 2005a, 2007), and Stevens (2005). The second approach relies on numerical simulations of magnetic dynamos. Such numerical experiments indicate that the magnetic moment may be independent on the angular frequency (Christensen & Aubert 2006; Olson & Christensen 2006). See also Cain et al. (1995) for a critical analysis of magnetic moment scaling laws.

Table 4 shows the size of the magnetospheric obstacle for various values of the planetary magnetic moment. We choose labels S1–S3 for values of the planetary magnetic moment that are obtained by the assumption that the planetary rotation has a strong influence on the planetary magnetic moment. Labels N1–N3 are used for cases which assume that HD 209458b is rapidly rotating. As the magnetic moment scaling laws are based on Jupiter, this is equivalent to saying that rotation rate has no influence on the magnetic dipole moment. Finally, we have, to enable a comparison, calculated which magnetic moment the values in Table 3 would correspond to. These values are labeled C1–C3. It is worth mentioning that, according to Equation (8),

Table 4
Magnetospheric Standoff Distance for Various Values of the Planetary Magnetic Moment (in Units of Jupiter's Magnetic Moment)

Case	\tilde{M}	$R_M [R_p]$
S1 ^a	0.05	2.3
S2	0.09	2.8
S3	0.17	3.5
N1 ^b	0.43	4.7
N2	0.46	4.8
N3	0.49	5.0
C1 ^c	1.0	6.3
C2	2.5	8.5
C3	4.9	11

Notes.

^a Cases S1–S3 are obtained with the formalism described in Grießmeier et al. (2007). They represent the minimum (geometrical), average, and maximum value expected for a tidally locked planet.

^b Cases N1–N3 are obtained with the same formalism, but assuming that the planet is rapidly rotating (i.e., with the same angular velocity as Jupiter).

^c The last cases C1–C3 are probably unrealistically high. They were calculated for comparison with Table 3.

the stellar wind parameters influence R_M only with a low exponent, and the result is thus not very sensitive to the choice of stellar wind parameters. For example, taking the stellar wind parameters of Grießmeier et al. (2007) rather than those of Table 1 modifies the numerical values in Table 4 by less than 10%.

The values of Table 4 can now be compared to those of Table 3. The comparison with Table 3 gives us that the magnetic moment of HD 209458b can be constrained to $5 M_{\text{Jup}}$ regardless of exospheric scenarios. And we also see that most scenarios would establish the magnetic moment of HD 209458b as smaller than M_{Jup} . The comparison with Table 4 shows that, with the current uncertainties on exospheric conditions, none of the cases S1–S3 and N1–N3 can currently be ruled out. However, if the exospheric conditions were certain a comparison would indicate which cases of planetary magnetic moments, S1–S3 or N1–N3 in Table 4, are more likely. If for example our default exospheric parameters are approximately correct we would have an estimation of the magnetic moment of HD 209458b as $\approx 0.4 M_{\text{Jup}}$. Within error margins, this value is compatible with the following interpretations: (1) planetary rotation is important for magnetic moment generation, but the true magnetic moment is close to the maximum value of the range predicted by the different scaling laws (case S3 in Table 4), or (2) planetary rotation is not as important as previously thought (cases N1–N3).

5. CONCLUSIONS

Holmström et al. (2008a) showed that the production of ENAs around HD 209458b can explain the observations reported by Vidal-Madjar et al. (2003). This work does a more detailed study of the ENA production around HD 209458b. Using an improved plasma flow model, we model the ENA production from charge exchange between stellar wind protons and exospheric hydrogen outside the obstacle boundary under stellar wind conditions similar to those at our Sun. Given uncertainties of the exospheric parameters we investigate their relative influence on the ENA production and determine an upper bound on the obstacle standoff distance for different values of exospheric density and temperature.

It was argued by Lecavelier des Etang et al. (2008) that the stellar velocity of 50 km s^{-1} assumed in Holmström et al. (2008a) was low. Compared to typical solar wind velocities, that is indeed a low value, and it was speculated that it might be due to the simplified flow model used (Holmström et al. 2008b). Here we have shown that the observed attenuation spectra during transit can be reproduced using a more typical stellar wind velocity of 450 km s^{-1} . Thus, ENA production can explain the observation using typical solar wind parameters. The absorption of atomic hydrogen as reported in Vidal-Madjar et al. (2003) can thus be explained by theory and conditions derived from our solar system. What is different from our solar system is, however, a close-in Jupiter-type planet, and from the ENA observations we try to extract information about the planet. The exospheric conditions and magnetic moment of HD 209458b are uncertain, and we study the ENA production for different exospheric conditions. We find that exospheric temperature is a more critical factor for the ENA production than exospheric density. If exospheric conditions were determined, the only remaining free parameter would be the obstacle standoff distance. For our assumed default exosphere we find that an obstacle standoff distance of $4.3R_p$ gives a good fit to observations. Depending on exospheric parameters an upper bound of the obstacle standoff distance is found at $(4.3\text{--}11)R_p$. Comparing the obtained obstacle standoff distances for the respective exospheric scenarios we see that the ENA observations could also provide information for exomagnetospheric modeling. Our simulations also show that the majority of tested exospheric scenarios would, with the available ENA observations, determine the magnetic moment of HD 209458b as smaller than that of Jupiter. With our default parameters we estimate the magnetic moment of HD 209458b to be approximately 40% of Jupiter's magnetic moment. The currently available data are not yet sufficient to put good limits on planetary magnetic moments. However, it seems possible that a more detailed modeling of exospheric conditions, together with improved ENA observations, could help to clarify the role of planetary rotation in the generation of planetary magnetic fields in the future.

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REFERENCES

- Ben-Jaffel, L. 2007, *ApJ*, **671**, L61
 Ben-Jaffel, L. 2008, *ApJ*, **688**, 1352
 Bird, G. A. 1976, *Molecular Gas Dynamics* (Oxford: Clarendon)
- Cain, J. C., Beaumont, P., Holter, W., Wang, Z., & Nevanlinna, H. 1995, *J. Geophys. Res.*, **100**, 9439
 Candy, J., & Rozmus, W. 1991, *J. Comput. Phys.*, **92**, 230
 Charbonneau, D., Brown, T. M., Latham, D. W., & Mayor, M. 2000, *ApJ*, **529**, L45
 Christensen, U. R., & Aubert, J. 2006, *Geophys. J. Int.*, **166**, 97
 Collier, M., et al. 2001, *J. Geophys. Res.*, **106**, 24893
 Desch, M. D., & Kaiser, M. L. 1984, *Nature*, **310**, 755
 Erkaev, N. V., Penz, T., Lammer, H., Lichtenegger, H. I. M., Biernat, H. K., Wurz, P., Grießmeier, J.-M., & Weiss, W. W. 2005, *ApJS*, **157**, 396
 Esser, R., Edgar, R. J., & Brickhouse, N. S. 1998, *ApJ*, **498**, 448
 Farrell, W. M., Desch, M. D., & Zarka, P. 1999, *J. Geophys. Res.*, **104**, 14025
 Fryxell, B., et al. 2000, *ApJS*, **131**, 273
 Futaana, Y., et al. 2006, *Icarus*, **182**, 413
 Galli, A., et al. 2008, *Planet. Space Sci.*, **56**, 807
 Garcia, A. L. 2000, *Numerical Methods for Physics* (Upper Saddle River, NJ: Prentice-Hall)
 García Muñoz, A. 2007, *Planet. Space Sci.*, **55**, 1426
 Grall, R. R., Coles, W. A., KlingleSmith, M. T., Breen, A. R., Williams, P. J. S., Markkanen, J., & Esser, R. 1996, *Nature*, **379**, 429
 Grenfell, J. L., et al. 2007, *Astrobiology*, **7**, 208
 Grießmeier, J.-M., Motschmann, U., Mann, G., & Rucker, H. O. 2005a, *A&A*, **437**, 717
 Grießmeier, J.-M., Stadelmann, A., Grenfell, J. L., Lammer, H., & Motschmann, U. 2009, *Icarus*, **199**, 526
 Grießmeier, J.-M., Stadelmann, A., Motschmann, U., Belisheva, N. K., Lammer, H., & Biernat, H. K. 2005b, *Astrobiology*, **5**, 587
 Grießmeier, J.-M., Zarka, P., & Spreeuw, H. 2007, *A&A*, **475**, 359
 Grießmeier, J.-M., et al. 2004, *A&A*, **425**, 753
 Henry, G. W., Marcy, G. W., Butler, R. P., & Vogt, S. S. 2000, *ApJ*, **529**, L41
 Hodges, R. R. J. 1994, *J. Geophys. Res.*, **99**, 23229
 Holmström, M. 2006, *Space Sci. Rev.*, **126**, 435
 Holmström, M., Ekenbäck, A., Selsis, F., Penz, T., Lammer, H., & Wurz, P. 2008a, *Nature*, **451**, 970 (H08)
 Holmström, M., Ekenbäck, A., Selsis, F., Penz, T., Lammer, H., & Wurz, P. 2008b, *Nature*, **456**, E2
 Khodachenko, M. L., et al. 2007a, *Planet. Space Sci.*, **55**, 631
 Khodachenko, M. L., et al. 2007b, *Astrobiology*, **7**, 167
 Kohl, J. L., et al. 1998, *ApJ*, **501**, 127
 Lammer, H., et al. 2007, *Astrobiology*, **7**, 185
 Lazio, T. J. W., Farrell, W. M., Dietrick, J., Greenless, E., Hogan, E., Jones, C., & Hennig, L. A. 2004, *ApJ*, **612**, 511
 Lecavelier des Etang, A., Vidal-Madjar, A., & Désert, J.-M. 2008, *Nature*, **456**, E1
 Lindsay, B. G., & Stebbings, R. F. 2005, *J. Geophys. Res.*, **110**, A12213
 MacNeice, P., Olson, K., Mobarry, C., deFainchtein, R., & Packer, C. 2000, *Comput. Phys. Commun.*, **126**, 330
 McComas, D. J., Elliot, H. A., Schwadron, N. A., Gosling, J. T., Skoug, R. M., & Goldstein, B. E. 2003, *Geophys. Res. Lett.*, **30**, 1517
 Olson, P., & Christensen, U. R. 2006, *Earth Planet. Sci. Lett.*, **250**, 561
 Penz, T., et al. 2008, *Planet. Space Sci.*, **56**, 1260
 Ralchenko, Y., Kramida, A. E., Reader, J., & NIST ASD Team 2008, NIST Atomic Spectra Database (Version 3.1.5; Gaithersburg, MD: National Institute of Standards and Technology), <http://physics.nist.gov/asd3>
 Russell, C. T., Baker, D. N., & Slavin, J. A. 1988, in *Mercury*, ed. F. Vilas, C. R. Chapman, & M. S. Matthews (Tucson, AZ: Univ. Arizona Press), 194
 Sheeley, N. R., Jr, et al. 1997, *ApJ*, **484**, 472
 Spreiter, J. R., & Stahara, S. S. *J. Geophys. Res.*, **85**, 6769
 Stevens, I. R. 2005, *MNRAS*, **356**, 1053
 Vidal-Madjar, A., Lecavelier des Etangs, A. L., Désert, J.-M., Ballester, G. E., Ferlet, R., Hébrard, G., & Mayor, M. 2003, *Nature*, **422**, 143
 Vidal-Madjar, A., Lecavelier des Etangs, A. L., Désert, J.-M., Ballester, G. E., Ferlet, R., Hébrard, G., & Mayor, M. 2008, *ApJ*, **676**, L57
 Vidal-Madjar, A., et al. 2004, *ApJ*, **604**, L69
 Voigt, G.-H. 1995, in *Handbook of Atmospheric Electrodynamics*, ed. H. Volland (Boca Raton, FL: CRC Press), 333
 Wurz, P. 2005, in *The Dynamic Sun: Challenges for Theory and Observations*, ESA SP-600, ed. D. Danesy et al. (Noordwijk: ESA), 1 (Chapter 5.2)
 Yelle, R. V. 2004, *Icarus*, **170**, 167
 Zarka, P., et al. 1997, in *Ground-based High Sensitivity Radio Astron. at Decimeter Wavelengths*, ed. H. O. Rucker, S. J. Bauer, & A. Lecacheux (Vienna: Austrian Academy of Sciences Press), 101